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 ^{16.} Abstract Time and reliability are two fundamental factors influencing travel behavior and demand. The concept of the value of time (VOT) has been extensively studied, and estimates of VOT have been obtained from surveys and empirical data. On the other hand, although the importance of value of reliability (VOR) is appreciated, research related to VOR is still in its early stages. The VOR has been estimated using surveys but has almost never been estimated using empirical data. This research used empirical data to take an initial step toward understanding the importance of travel time reliability. Katy Freeway travelers face a daily choice between reliable tolled lanes and less reliable but untolled lanes. An extensive dataset of Katy Freeway travel was used to examine the influence of time, reliability, and toll on lane-choice behavior. Lane choice was estimated using multinomial logit 			ned from (VOR) is using surveys of travel ess reliable ence of tial logit	
models. Basic models, including only travel time and toll, yielded reasonable results. Models included VOTs of \$2.60/hour, \$8.63/hour, and \$10.71/hour for off-peak, shoulder, and peak-period travelers, respectively.				
However, adding a managed-lane (ML) alternative specific coefficient to these models resulted in positive coefficients for the toll variable and negative VOTs. Similarly, adding reliability to the models resulted in counter-intuitive results. Researchers concluded that additional research on how travelers perceive the reliability and time savings on MLs is needed because modeling real-world choices of MLs using the standard definitions of reliability and time savings led to counter-intuitive results.			ls resulted in ceive the	
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EMPIRICAL MEASUREMENT OF TRAVELERS' VALUE OF RELIABILITY

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EXECUTIVE SUMMARY

Time and reliability are two fundamental factors influencing travel behavior and demand. The concept of the value of time (VOT) has been extensively studied, and the VOT has been estimated using surveys and empirical data. However, research related to the value of reliability (VOR) is still in its early stages. The VOR has been estimated using surveys but has almost never been estimated using empirical data.

This research used empirical data to take an initial step toward understanding the importance of travel time reliability. Katy Freeway travelers face a daily choice between reliable tolled lanes and less reliable but untolled lanes. A dataset of Katy Freeway travel in April 2012 was used to document travel behavior and examine the influence of time, reliability, and toll on lane-choice behavior. This dataset was modified to make it impossible for researchers to identify a specific traveler; each traveler was given a unique random ID number.

Based on the data, researchers found that most paid trips on the managed lanes (MLs) occurred during the peak hours, followed by the shoulder hours and off-peak hours. For each trip identified on the freeway, an alternate trip on the lanes not chosen was developed using the prevalent conditions to create a choice set. For example, when the actual trip was on the general-purpose lanes (GPLs), an alternate trip was created on the tolled lanes with the characteristics of travel (travel time, reliability, and toll) at that exact time on the tolled lanes. In this way, travel information regarding the trip taken and the trip not chosen was developed. Lane choice was estimated using multinomial logit models. Basic models, including only travel time and toll, yielded reasonable results. Models included VOTs of \$2.60/hour, \$8.63/hour, and \$10.71/hour for off-peak, shoulder, and peak-period travelers, respectively.

However, adding an ML alternative specific coefficient (ASC) to these models resulted in positive coefficients for the toll variable and negative VOTs. Similarly, adding reliability to the models resulted in counter-intuitive results. In all models, addition of the ASC led to relatively high ASC values (in magnitude) compared to other attribute coefficients, indicating a weak relationship between lane choice and model attributes. Researchers concluded that additional research on how travelers perceive the reliability and time savings on MLs is needed because modeling real-world choices of MLs using the standard definitions of reliability and time savings led to counter-intuitive results.

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CHAPTER 1: INTRODUCTION

Understanding and modeling traveler behavior are the cornerstone of transportation planning. Good planning, in turn, results in sustainable investments in infrastructure and increased economic competitiveness. Travelers make travel decisions based on their understanding and perception of different influencing factors such as the value of time (VOT), comfort, or safety. Predicting how travelers will behave when faced with a choice between a potentially congested but toll-free route and an uncongested but tolled route is particularly challenging. Part of this challenge comes from not understanding the value travelers place on the more reliable travel times offered by the tolled route. A substantial effort is underway by the U.S. Department of Transportation (USDOT) through the Strategic Highway Research Program 2 (SHRP 2) to incorporate travel time reliability into the planning process. In addition, many stated-preference surveys have been undertaken to estimate travelers' value of reliability. Despite these efforts, researchers are still not sure how travelers perceive or value travel time reliability.

Managed lanes (MLs), a component of congestion management, are defined as highway facilities or a set of lanes in which operational strategies are implemented and managed (in real time) in response to changing conditions to preserve unimpeded flow. Often MLs operate alongside free general-purpose lanes (GPLs) in order to allow travelers to choose between the two lanes. High-occupancy vehicles (HOVs) are encouraged in these systems by being allowed to use the tolled lanes either toll free or at a reduced rate. These types of MLs are becoming increasingly popular in the United States and are now present in multiple cities across the country.

Katy Freeway Dataset

Houston's Katy Freeway is one such ML facility that became operational in 2008. This project tries to understand how travelers value travel time reliability using empirical travel data from Katy Freeway travelers in Houston. The dataset consists of records generated from automated vehicle identification (AVI) sensors placed at regular intervals along the freeway. The data were processed to generate travel times and identify lane choices for every single trip identified on the freeway. This means that not only are the average travel times of the vehicles on the roadway known, but so is the travel time of a particular vehicle on any of its Katy Freeway trips through the identification of its unique transponder. This dataset is unique because Katy Freeway is one of the few freeways that have both tolled and free lanes, and that have AVI readers on both sets of lanes. These data were combined with crash data, lane blockages, weather, and toll rates—the many factors that could potentially impact travel time and travel time reliability. This provided an unmatched dataset of travel conditions on GPLs and MLs.

This dataset was then used to calculate the reliability of travel times on the freeway. Attributes such as time, toll, and reliability were used to run multinomial discrete-choice models and to

study the relative importance of these variables in the decision-making process. The travel behavior witnessed provided insight into how much travelers are willing to pay for the travel time savings and reduced travel time variability of the MLs.

Research Objectives

The design of Katy Freeway (two MLs and at least four GPLs in both directions) provides an ideal real-world environment to study how travelers choose between faster, more reliable tolled lanes and congested, less reliable untolled lanes over an extended period of time. This understanding can assist planners in making better decisions to provide sustainable and economically viable transportation options.

The emphasis of this project was understanding and modeling how travelers behave when given a choice between more reliable tolled lanes and less reliable untolled lanes on a daily basis. The project had the following objectives:

- 1. Document the travel behavior of individual travelers on both the toll lanes and GPLs on a freeway using empirical data.
- 2. Examine factors that influence how travelers make lane-choice decisions, and the relative importance of these factors.
- 3. Estimate an empirical value of travel time reliability.
- 4. Estimate a value of travel time that is separate from the value of travel time reliability.

CHAPTER 2: LITERATURE REVIEW

Travel time can be defined as the time elapsed when a traveler travels between two (distinct) spatial positions (Carrion and Levinson, 2012a). Travel time is typically easily understood because it is a one-dimensional quantity. Travel time reliability, on the other hand, is a concept related to the unpredictability of travel time between two spatial points. It is a measure of the spread of the travel time distribution. In simple terms, the greater the variation in travel time between two points, the less reliable it is and vice versa. Therefore, the concept of travel time (un)reliability is used interchangeably with travel time variability in transportation literature. According to Wong and Sussman (1973), this unpredictability of travel time can be attributed to:

- Variations between seasons and days of the week.
- Variations because of change in travel conditions due to weather, accidents, etc.
- Variations attributed to each traveler's perception.

The VOT and value of reliability (VOR) are measures of travelers' willingness to pay for reducing their travel time and improving the predictability (i.e., reducing travel time variability) of their trip. These are two fundamental factors influencing travel behavior and demand. Therefore, considerable efforts have been made to better understand these factors to improve the transportation planning and decision-making process.

Value of Travel Time

The literature on the value of passenger travel time is extensive and well developed. The earliest studies on the VOT date back to the 1960s (Becker, 1965; Beesley, 1965; Oort, 1969). Values of travel time have most often been determined by estimating mode-choice models and evaluating the marginal rates of substitution between the costs and travel times of the alternative modes. The VOT increases as travelers shift from congested to uncongested travel (Small et al., 1999).

Cherlow (1981) listed various studies conducted on the evaluation of the VOT. The estimated VOT varied from as low as 9 percent of the wage rate to as high as 140 percent of the wage rate. He suggested that there is no single VOT that can be applicable to all people in all circumstances. A study by Lam and Small (2001) estimated the average VOT to be \$22.87/hour, or 72 percent of the average wage rate. Patil et al. (2011) estimated the VOT for different situations on MLs, including one normal and six urgent situations. Patil et al. found that travelers place a higher value for travel time savings when in an urgent travel situation than in a normal situation—well over 100 percent of the wage rate.

Few studies in the recent literature try to estimate the VOT on MLs. A study by the Georgia Department of Transportation (GDOT) using a stated-preference survey estimated the VOT of passenger car travelers to be in the range of \$7/hour to \$15/hour. GDOT also observed that the

VOT varied with the type of vehicle. Drivers of six-axle vehicles valued travel time savings at a higher price than drivers of passenger cars (GDOT, 2010). A more recent study on I-25 travelers in Miami by the Florida Department of Transportation estimated the VOT as 49 percent of the hourly wage, with a range of \$2.27/hour to \$79.32/hour and a mean value of \$32/hour (Perk et al., 2011).

Value of Travel Time Reliability

Research attempting to quantify the VOR is relatively new. Although it has received increased attention, the procedure for quantifying the VOR and the estimated values are still a topic of debate (Carrion et al., 2012a). No acceptable valuation exists thus far because existing valuations of the VOR must be examined in light of the underlying assumptions of the study. Three distinct theoretical frameworks have been examined to understand the value of travel time reliability:

- Centrality dispersion.
- Scheduling delays.
- Mean lateness.

The centrality-dispersion framework, in a transportation context, is based on the notion that both expected travel time and travel time variability are sources of disutility:

$$U = \gamma_1 \mu_T + \gamma_2 \sigma_T \tag{1}$$

Where: U = expected utility.

 μ_T = expected travel time.

 $\sigma_{\rm T}$ = dispersion measure of travel time distribution.

 $\gamma_{1,2}$ = coefficients.

Therefore, the traveler is minimizing the sum of the two terms: the expected disutility of travel time and the travel time variability of the trip.

The scheduling-delay framework is based on the costs associated with early or late arrival relative to arrival time constraints (e.g., work start time). The travelers' intrinsic choice of a preferred arrival time is the point of reference that delimits if an arrival is early or late. Scheduling decisions made for a given probability density distribution of trip delay and the associated costs are used to determine how travelers value travel time reliability.

The mean-lateness framework is based on the expected utility paradigm. Used primarily for transit, the framework consists of two elements: schedule journey time and mean lateness at arrival. The schedule journey time is the time between scheduled arrival and scheduled

departure. The lateness is the sum of lateness at boarding and lateness at arrival. Train fares are added to calculate the marginal rates of substitution between temporal quantities and travel cost.

Among the three, centrality dispersion has been the most popular among researchers. Most studies pertaining to the VOR can be categorized as stated-preference studies or revealed-preference studies.

Stated-Preference Studies

To date, stated-preference (SP) techniques have proven to be the most valuable tool for estimating the value of travel time reliability. In their survey, Black and Towriss (1993) asked respondents to choose between distinct options with a varying spread of travel times, mean travel times, and travel costs. They found travel time variability to be a significant factor although the magnitude was found to be smaller than the mean VOT (0.55 times VOT). Black and Towriss also introduced the concept of a reliability ratio (RR), given by:

$$RR = \frac{VOR}{VOT}$$
(2)

Small et al. (1999) used mean-variance models, scheduling models, and combined models to estimate the VOR. In their survey design, the concept of travel time variability was presented using a text-only format (see Figure 1). The respondents were asked to choose between two scenarios with the same average travel time but different costs and different travel time distributions. Researchers found the VOR on average to be 3.22 times the VOT in congested conditions.

In the late 1990s and 2000s, more attention was devoted to designing better presentations of questions that included variability. Hensher (2001) used bar diagrams to present the concepts of time and reliability to survey respondents. He divided the total travel time into free flow, slowed down, stop/start, and uncertainty allowance (see Figure 2). This was because he was more concerned about the values that travelers assign to each distinct component of travel time rather than general travel time reliability. Three scenarios were provided with varying travel time components and travel costs.

Copley and Murphy (2002), through their qualitative research, found that histogram presentations could present a large volume of information and were understood with little effort by the respondents (see Figure 3). In their survey, the respondents were presented with two choices with varying arrival time distributions.

Tseng et al. (2009) compared the presentation of variability in various studies by conducting face-to-face interviews with subjects to study their understanding of the concepts. Researchers found that the format used by Small et al. (1999) (shown in Figure 1) was understood by most of the respondents and was the most preferred form of presentation.

PLEASE CIRCLE EITHER CHO	DICE A OR CHOICE B
Average Travel Time: Average Travel Time	
9 minutes	9 minutes
You have an equal chance of	You have an equal chance of
arriving at any of the follow-	arriving at any of the follow-
ing times:	ing times:
7 minutes early	3 minutes early
4 minutes early	3 minutes early
1 minute early	2 minutes early
5 minutes late	2 minutes early
9 minutes late	On time
your cost: \$0.25	your cost: \$1.50
Choice A	Choice B

Figure 1: Text-Only Presentation of Variability from Small et al. (1999).

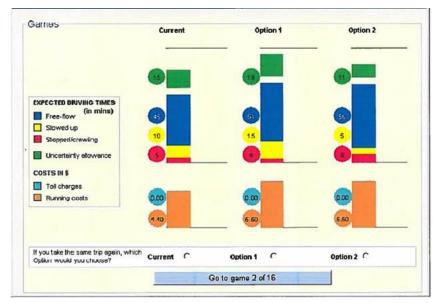


Figure 2: Bar-Diagram Presentation of Variability from Hensher (2001).

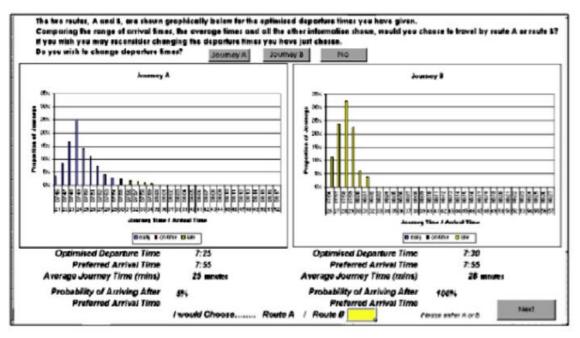


Figure 3: Histogram Presentation of Variability from Copley and Murphy (2002).

Li et al. (2010) derived the value of reliability, scheduling costs, and reliability ratios in the context of Australian toll roads. They used the SP survey to study how travelers in Australia make trade-offs between different levels of travel times and reliability with tolls and vehicle-running costs. They found a mean estimate for early expected schedule delay to be AUS \$24.1/hour and a mean estimate for late expected schedule delay of AUS \$38.86/hour. The mean VOR from the mean-variance model was AUS \$40.39/hour. Unlike in other studies, their study focused on both commuters and non-commuters. A recent study by Tilahun and Levinson (2010) found that the travelers' value travel time reliability was very close to their VOT.

Carrion and Levinson (2012a) pointed out that in most SP studies, researchers have not validated whether the respondents' understanding of the abstract situation matches the analysts' intentions of the abstract situation. Therefore, it is difficult to ascertain which measures of travel time variability are more plausible than others. Also, the survey design may affect the reliability estimates due to the difficulty of presenting the concept of travel time reliability to subjects without any statistical background.

Devarasetty et al. (2012) studied the value travelers place on travel time reliability by comparing SP survey data and actual usage data of Katy Freeway travelers. For the survey, approximately half of the respondents received questions in picture format, while the other half received questions in the text-only format. Each question in the survey had four travel choices:

- Drive alone on GPLs.
- Drive alone on toll lanes.

- Carpool on GPLs.
- Carpool on toll lanes (see Figure 4).

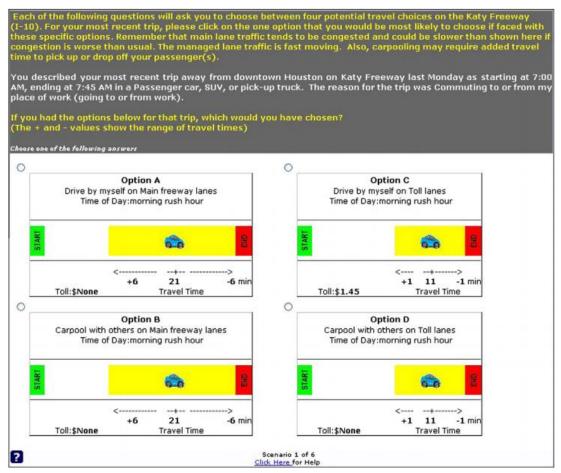


Figure 4: A Typical Scenario in Picture Format from Devarasetty et al. (2012).

Trips on the toll lanes (which had a toll of \$1.45 if driving alone and were free if carpooling) were shown to be faster and more reliable than trips on the GPLs. The respondents' choices were similar for both formats, implying that both formats were similarly understood. Three stated-choice experiment design techniques were tested to develop logit models: Bayesian (Db) efficient, random level attribute generation, and adaptive random approach. The Db-efficient design was superior to the other two techniques. Researchers found the combined estimate of the VOT and VOR based on the SP survey (Db-efficient design) to be \$50/hour, which was very close to the estimated VOT of \$51/hour from actual usage. This implied the calculated VOT using actual usage data includes the value travelers place on reliability plus the value of travel time savings on the MLs.

Concas and Kolpakov (2009) reviewed the literature on the VOT and VOR and recommended that the VOR be estimated at 80 to 100 percent of the VOT under ordinary travel circumstances with no major travel constraints. The most recent investigation of VOR undertaken by the

Netherlands Institute for Transport Policy Analysis (2013) used a large SP survey to determine that the VOR ranged from 40 percent of the VOT for commute trips to 110 percent of the VOT for business trips.

Revealed-Preference Studies

Revealed-preference (RP) studies are few in number in comparison to SP studies. The primary reason is the lack of experimental settings in the real world that provide an opportunity to observe travelers choosing between routes with different travel time reliabilities for a toll. RP studies can be divided into two categories based on how travel time data are measured:

- Subjective travel time measurements, which use travel time as reported by the respondents.
- Objective travel time measurements, which use travel time as obtained from devices such as global positioning systems (GPS) and loop detectors.

A few early studies on the value of reliability using actual traveler usage data were from State Route (SR) 91 in Orange County, California. Travelers chose between a free (less reliable) and variably tolled (more reliable) route. Lam and Small (2001) measured the value of reliability using 1998 loop detector data as well as surveying a sample of the travelers. Using loop detector data, Lam and Small were able to estimate the average travel time within 15-minute intervals. Through the survey of their sample group (533 respondents), Lam and Small were able to gather information about travelers' most recent weekday trip. Unfortunately, the loop detector data were from one year prior to the survey. Therefore, the researchers had to approximately adjust the travel times by using the trends observed in the congestion data. Also, the travel times obtained using the loop detector data were averaged over 15 minutes and were therefore not representative of the specific travel time of a trip maker. Lam and Small found that the best-fitting models represented travel time by the difference between the 90th percentile and the median. In their best models, the value of reliability was \$15.12/hour for men and \$31.91/hour for women. These values were 48 percent and 101 percent, respectively, of the average wage rate in the sample. Because the average wage rates of the sample were used, these figures are not necessarily representative of how much each individual values travel time reliability relative to his or her wage rate.

Small et al. (2005, 2006) combined both RP (actual preferences of lane choice) and SP (hypothetical scenarios to better understand lane choice) observations of travelers on SR 91. The data were collected using telephone interviews and mail-back surveys. The researchers noted that RP data collected using surveys are affected by perception errors and therefore can never be completely representative of the real-world scenario. Also, 522 individuals took the RP survey, and 633 took the SP survey, but only 55 respondents took both. Therefore, combining data from different individual may have introduced errors in the study. The researchers calculated the

median VOR using the RP data of travelers in Los Angeles and estimated the median VOR to be 85 percent of the average wage rate (\$19.56/hour). The researchers also found the heterogeneity in travel time and reliability to be significant. Brownstone and Small (2005), using the data from SR 91 and I-15 high-occupancy toll (HOT) lanes, estimated the VOR to be 95 to 140 percent of the median travel time.

In another study, Carrion and Levinson (2012b) estimated the value placed on the HOT lanes because of improvements in travel time reliability from a GPS-based experimental design. the researchers recruited 18 regular commuters on the I-394 MnPass lanes in Minnesota and equipped them with GPS devices. For the first two weeks, these commuters were instructed to travel on each of the three alternatives (HOT lanes, untolled lanes [GPLs], and nearby signalized arterials) and then were given the opportunity to travel on their preferred route after experiencing each alternative. The researchers found that reliability was valued highly in each of the models but was valued differently according to how it was defined (standard deviation, shortened right range, and interquartile range). Though the study used RP data, the low number of participants in the experiment design may have biased the results.

Variation in Studies

From the discussion in the previous sections, it is clear that large variations in estimates have been found across different studies. These differences in the valuation of travel time reliability are a key problem in comparing estimates across studies. Tseng and Verhoef (2008) classified the main differences into the following categories:

- Data type (RP, SP, and joint RP and SP).
- Scheduling versus reliability measures.
- Various travel time reliability measures (e.g., standard deviation and interquartile range).
- Travel time unit.
- Presence of heterogeneity (observed and unobserved).
- Choice dimensions (e.g., mode and route).

The data type differences are primarily the difference in SP, RP, and actual usage studies. SP studies are affected by the perception of the VOR of respondents and their understanding of abstract concepts. Often in RP and actual usage studies, there is simply not enough variation in tolls to be able to empirically determine the influence of cost on decision making (Devarasetty et al., 2012). Scheduling and reliability measures are closely related and thus obscure the contribution of each other in model estimates. Differences in reliability measures lead to variation in results. Different reliability measures, such as standard deviation, difference in 90th and 50th percentiles, etc., have been used in studies. Heterogeneity in the subjects of studies (e.g., socio-economics attributes) can lead to varying results across studies. These factors interact with the travel time, reliability, and cost terms, making it difficult to estimate the valuation

ratios. Finally, differences in the choice behavior of travelers between mode, route, and departure time may influence the estimation of the VOT and VOR. This means the lack of homogeneity in the experiment design of various studies potentially leads to variations in the results.

About This Research

The methodology in this project aims to address most of the issues faced in previous studies of travel time reliability. Using actual freeway usage data, instead of surveys, eliminates the concerns of survey-based studies. It also provides the actual choices travelers made, thus eliminating perception errors induced in SP survey studies. Also, the data allow for an estimate of the value of travel time that is separate from the value of travel time reliability.

As discussed, some RP studies have tried to incorporate actual usage data to validate or improve their model estimates. The main problem with these studies is the collection of usable travel time data. Loop detectors, in-field measurements (e.g., driving in similar time periods), and GPS devices have been used. Loop detectors require several assumptions and processing to estimate travel time. In-field measurements are easier to get but do not reflect actual travel times. GPS devices measure very detailed commute-level data but are difficult to obtain. This research overcomes these problems by using highly accurate AVI data to identify trip times on both MLs and GPLs. Moreover, previous studies that used RP data and actual usage data had to approximate travel times using algorithms and could not obtain the actual travel time of the specific respondent being surveyed in the RP survey (Lam and Small, 2001; Small et al., 2005, 2006). In this project, accurate travel times for each individual traveler with a transponder identification (ID) number were available (on both the MLs and GPLs), and no approximation of travel times was needed.

Another reason for variation in results among different studies is the influence of time of day over travel time. Measures from off-peak hours may differ from those during the peak hours. The dataset for this project was used to identify travel times during all hours of the day with no exception. This enabled researchers to generate separate datasets based on the time of day and develop different models to understand variations in results, if any, due to the time of day.

CHAPTER 3: DATA

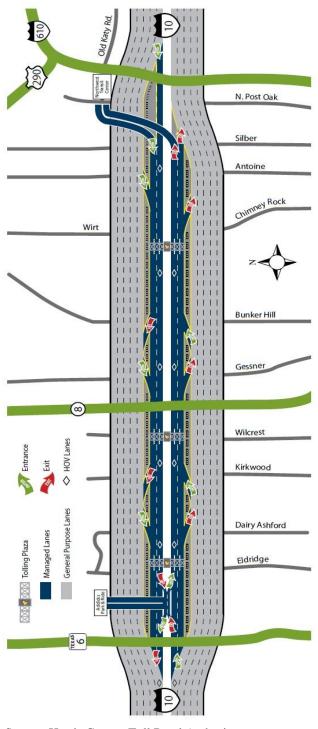
Katy Freeway

Katy Freeway is one of Houston's major highways and connects the city of Katy in the west to downtown Houston in the east. The highway has a total length of 40 miles and was constructed in the 1960s. The initial design had three lanes per direction and two frontage lanes to accommodate approximately 80,000 vehicles per day.

In the late 1990s and early 2000s, traffic volumes started reaching three times the volume the highway could serve, which resulted in chronic congestion levels lasting up to 11 hours a day. This led to the Texas Department of Transportation (TxDOT) undertaking a major five-year reconstruction project for a 12-mile section of the freeway between just west of SH 6 and the I-10/I-610 interchange. The project broke ground in 2003 and was completed in October 2008. This \$2.79 billion project was partially funded through a combination of state funds, federal funds, and toll receipts.

The reconstruction widened the 12-mile stretch to provide up to six GPLs in each direction and two variably priced MLs in the median of the highway. Figure 5 is a detailed map of Katy Freeway. The two lanes in the middle running in both directions are MLs with four entry and four exit points in both directions. HOVs with two or more occupants and motorcycles do not have to pay a toll during the HOV-free hours but have to pay the same toll rate as single-occupancy vehicles (SOVs) during all other hours. HOV hours are Monday through Friday 5 a.m. to 11 a.m. and 2 p.m. to 8 p.m. This is done to encourage ride sharing and increase vehicle occupancy. HOVs must also be in the HOV lane (inside lane) of the MLs to avoid the toll during the HOV-free hours. GPLs have no tolls at any time. In general, the MLs provide faster and more reliable travel times compared to the GPLs.

The freeway has three tolling plazas (near the cross streets of Eldridge, Wilcrest, and Wirt) for toll collection from vehicles. All toll collection at these booths is done electronically, and vehicles need to have transponders in order to use the toll lanes. All vehicles passing through any toll booth are identified with the help of the transponder and are charged a toll depending on the time of the day and the toll plaza. The operation and toll collection for the freeway are handled by the Harris County Toll Road Authority (HCTRA).



Source: Harris County Toll Road Authority Figure 5: Katy Freeway.

To legally use the MLs, SOVs must pay a toll, which varies by time of day. The toll rates that were in effect during the period of analysis are shown in Table 1.

Time Period	Toll Plaza		Toll Plaza		
Time Feriod	At Wilcrest	At Wirt	At Eldridge		
Peak Period					
(7–9 a.m. Eastbound and	\$1.20	\$1.20	\$1.60		
4–6 p.m. Westbound)					
Shoulder					
(6–7 a.m. and 9–10 a.m.					
Eastbound and	\$0.60	\$0.60	\$0.80		
3–4 a.m. and 6–7 p.m.					
Westbound)					
Off-Peak Period	¢0.20	\$0.60	¢0.40		
(All Other Times)	\$0.30	\$0.60	\$0.40		

Table 1: Toll Schedule on Katy Managed Lanes (April 2012).

All along the freeway, in both directions, AVI sensors are placed along the MLs, GPLs, and frontage road lanes. The section of highway examined in this research had 38 readers owned and operated by TxDOT (see Figure 6). Each sensor is assigned a unique number, which is used to identify the location and direction of travel of vehicles passing the sensor. Only vehicles with a valid transponder ID are detected at these sensors. Upon detecting a vehicle, the sensor records the time of detection and the unique transponder ID of the vehicle. For this project, these data and the location of the sensors were used to identify vehicle trips on the freeway. Each transponder ID was assigned a unique random number, and the original ID was deleted. In this way, it was impossible to trace the records back to the driver who made the trip. Figure 6 shows the location of the AVI sensors.

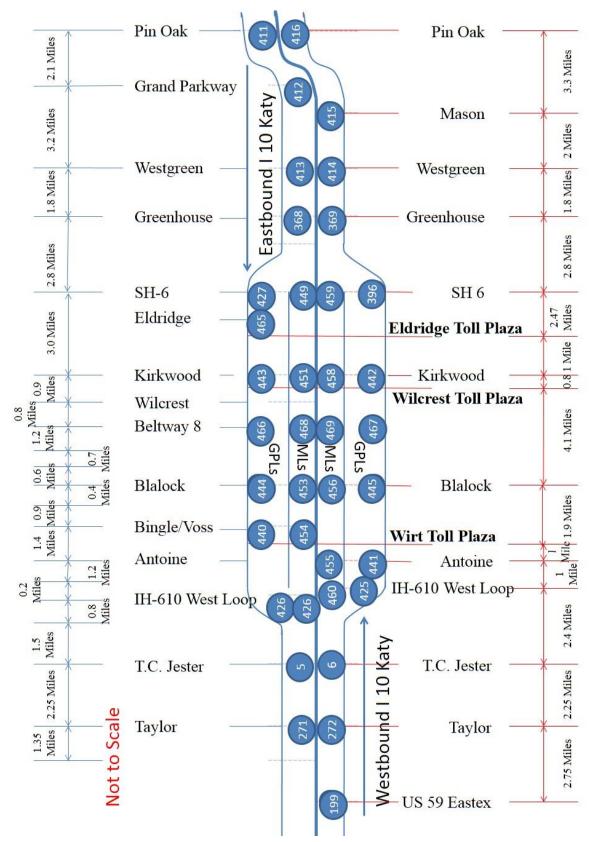


Figure 6: Katy Freeway AVI Sensor Locations.

Data Sources

AVI Data

The AVI or automatic vehicle identification data contain all sensor detection records of vehicles with transponders on Katy Freeway for 2012. These data were obtained from TxDOT. Each record has the time stamp, the sensor number, and the unique vehicle transponder ID. The data were processed and used to identify trips on the MLs and GPLs. The dataset was modified to make it impossible for the researchers to identify a specific traveler. The dataset was combined with the HCTRA toll data, and then each transponder ID was assigned a unique random ID number. When the researchers were satisfied the randomizing process worked correctly, the original data and the randomizing code were deleted, making it impossible to identify the original transponder ID and the person who took a particular trip.

For 2012, 225,118,768 records were obtained from the 38 readers on Katy Freeway. This amounted to 1,993,347 unique transponder ID detections for the entire year. For April, 870,819 unique transponder IDs were detected on the freeway, and 4,496,918 trips were identified in both directions.

HCTRA Toll Data

The tolling dataset for 2012 was obtained from HCTRA, which used the data to charge the vehicle the appropriate toll rate based on the toll schedule. The dataset contained all vehicles with valid transponder IDs that were detected at the toll plazas along the MLs on Katy Freeway. Each record in the dataset contains the time stamp of detection, the unique transponder ID of the vehicle detected, location, toll plaza ID number, and lane ID number. For the purpose of this project, these data were used to supplement the AVI detections in order to better identify trips along the MLs. In the trip identification algorithm, these data were also used to assign the correct toll rate to each trip identified on the MLs or properly identify non-tolled vehicles in the case of toll-free HOVs on the MLs.

For 2012, 14,769,730 toll detection records were generated, with 1,310,043 during April 2012.

Crash and Lane Closure Data

TxDOT provided a dataset containing information pertaining to all incidents (including crashes) and resulting lane closures on Katy Freeway for 2012. This dataset was included to factor in the impact of lane closures on travel time, travel time reliability, and decision making of the traveler. In theory, the impact of crashes on travel time and travel time reliability was already accounted for with the data collected on those two variables. However, radio and Internet announcements of lane closures may have impacted travel, and so lane closures were included as independent variables.

The dataset contained information about the type of incident, type of lanes affected (ML, GPL, or frontage), number of lanes affected, duration for which lanes were affected, and location of the incident. Researchers then identified the nearest sensors to the site of the incident. For 2012, 1,178 incidents were recorded. Of these, 36 records had incomplete information and were therefore deleted. All the incidents led to at least one lane being blocked on the freeway system. For April, 121 incidents were recorded, and these were the only ones included in the analysis.

Weather Data

Data pertaining to hourly rain information were obtained from the National Climatic Data Center. The dataset contained the hourly rainfall level in inches near Katy Freeway. A variable to identify heavy rain was incorporated in the dataset when recorded rainfall was greater than 0.4 inches in an hour. In April 2012, there were four such hours with more than 0.4 inches of precipitation.

Research Methodology

For this project, only one month of data was used due to the volume of trips and the computational power needed to deal with the analysis. April was chosen because it was a fairly typical traffic month, it was before the summer when traffic decreases on Katy Freeway, and it was well before the toll changed in September 2012.

Achieving the objectives of this research required a set of empirical data that included a majority of the attributes used by travelers to choose between a priced and reliable set of lanes (MLs) versus an unpriced (or lower priced) but less reliable set of lanes (GPLs). Using the datasets mentioned in the previous section, a new dataset for April containing all the identified trips and all the possible attributes that could be ascertained was created. Some of the trip attributes included were the random ID of the vehicle, travel time, toll paid, travel time standard deviation, time of day when the trip was made (peak or off-peak), and trip length. For all the trips identified on the freeway, a second trip was generated on the lanes not chosen (i.e., GPL for ML trips and ML for GPL trips). The attributes for this dummy trip were calculated using the information available from trips that were made on those same lanes at the same time (a 15-minute window).

Since it is unclear how travelers perceive travel time reliability, different variables can be used to represent travel time reliability. For this project, the standard deviation of travel time was used as a measure of travel time reliability. In other words, the higher the standard deviation, the less reliable the trip would be.

Obtaining a dataset that includes every attribute a traveler might use in choosing between these two set of lanes would be impossible. Thus, a methodology that allows for some unknown attributes and their impacts was needed. Logit models were used to estimate lane-choice behavior (GPL versus ML). A logit model is a type of regression analysis used for predicting the

outcome of a categorical dependent variable based on one or more predictor variables. In this project the dependent variable is binary (ML or GPL), and therefore the logit model is called a binary logit model. The following is an example of the type of logit model used in this project:

 $U_{GPL} = \beta_{TT} TravelTime_{GPL} + \beta_{TTR} TravelTimeReliability_{GPL} + \beta_{GLB} GPLsBlocked$ $U_{ML} = \beta_{ML} + \beta_{TolIML} Toll_{ML} + \beta_{TT} TravelTime_{ML} + \beta_{TTR} TravelTimeReliability_{ML} + \beta_{LB} MLsBlocked + \beta_{rain} Rain$ (3)

Where: U_i = utility derived by choosing lane i.

β_i = coefficient associated with attribute i.
GPL = general-purpose lane.
ML = managed lane.
Toll = toll paid on the toll lane.
TT = travel time.
TTR = travel time reliability.
GLB = GPLs blocked.
MLB = MLs blocked.

The VOT and value of travel time reliability could then be obtained by comparing the relative importance of attributes related to travel time, travel time reliability, and toll in determining lane choice.

CHAPTER 4: DATA ANALYSIS

This chapter briefly discusses the algorithm that was used to identify the trips and trip attributes. It also outlines all the assumptions that were made and their impact on the analysis, and clearly explains the final dataset that was obtained.

Cleaning, Merging, and Randomization of Data

The first step of the analysis was to clean the raw data. No records with incomplete information were found in the AVI and HCTRA data, but a small number of duplicate entries were found and removed.

Toll data were modified to be merged with the AVI sensor data. In the original dataset, each toll booth was identified by a plaza ID. In order to enable the merge, each toll booth was assigned a sensor number instead of the plaza ID to match the AVI sensor data. All attributes other than the time stamp, sensor number, and transponder ID were removed.

After the merge, all transponder IDs were assigned a unique random ID, and the original transponder ID was deleted. This ensured no trip could be mapped back to the original transponder ID. This randomized dataset was used for all subsequent analysis.

Records corresponding to random IDs that were detected only once (that is, a single location) were deleted because no trip could be identified by a single detection. Therefore, a dataset with only random IDs that were detected more than once was created. After these initial steps, the total number of records (individual transponder reads) for the whole year was 225,118,768. For April, the total number of records was 19,383,952.

Trip Identification

Records were sorted in chronological order and according to random ID. Therefore, consecutive detections, one after the other, for the same random ID were chained together to trace a trip through the freeway. For example, a specific vehicle transponder identified at readers 413, then 368, then 443, and finally 444 within a given time period was converted into a single trip entering the freeway at reader 413 and exiting at reader 444 (refer to Figure 6). If the time difference between two consecutive detections for the same random ID was greater than 10 minutes, the two detections were considered to be part of two different trips.

Trip times were calculated by taking the difference in time between the first detection and the last detection. Similarly, trip length was calculated by measuring the distance between the location of the first and last sensors. Distances between all sensors were calculated using Google Earth and are shown in Figure 6.

A toll was assigned to a trip that had at least one detection at one of the toll plazas. The tolls were assigned according to the time of detection and the corresponding toll value in the toll schedule. No toll was applied to the trip if the vehicle was detected on the HOV lane portion of the MLs during the HOV-free hours. The total toll for the trip was equal to the sum of tolls paid along the trip at up to three different toll booths.

Estimation of Trip Standard Deviation

As mentioned in the previous chapter, travel time reliability was defined as the standard deviation of travel time. The travel time standard deviation was calculated per 15-minute interval for each sensor pair using all the trip times during that 15-minute interval for that sensor pair. Despite the large number of trips in the dataset, there were some 15-minute periods when there were too few trips to determine the standard deviation on one set of lanes (GPLs or MLs). When there were very low volumes of traffic (two or fewer vehicles per 15-minute period) on the lanes, the standard deviation for that sensor pair was allowed to be zero. When there was traffic on the lanes but that particular sensor pair did not experience enough trips, the standard deviation was estimated by using the regression equation shown in Equation 4:

$$\sigma_{X,Y} = 0.48 \times \sum_{i} (\sigma_i) + 2.20 \times S + 6.37 \tag{4}$$

Where: $\sigma_{X,Y}$ = standard deviation of travel speeds between sensor pair X, Y of the roadway.

 σ_i = standard deviation of speeds for all adjacent sensor pairs located between sensor pair X,Y.

S = number of adjacent sensor pairs between sensor pair X,Y.

For example, the standard deviation for a trip that starts at sensor 413 and ends at sensors 444 while going through sensors 368 and 443 is given by Equation 5:

$$\sigma_{413,414} = 0.48 \times (\sigma_{413,368} + \sigma_{368,443} + \sigma_{443,444}) + 2.20 \times 3 + 6.37 \tag{5}$$

This regression equation was calculated by using data from all the sensor pairs, for all those 15-minute periods where at least five trips were identified between the given sensor pair. The entire month's data were used to develop the regression equation. This amounted to 2,576,194 data points. The regression model had an R-squared value of 0.49. A number of different models were tried to improve the R-squared value, but no significant improvement was observed. Different models for the peak, off-peak, and shoulder were developed. Step-wise regression was tried with a large number of trip variables, but in both cases, the complexity of the model increased significantly without a commensurate increase in the R-squared value. A model with only the sum of the standard deviation of speeds was also tried, but the model had a lower R-square than the one for Equation 5.

Alternate Trip Generation

An alternate trip was generated to develop attributes for the lane that was not chosen. This means for every trip made on the MLs, an alternate trip was created on the GPLs and vice versa. This was necessary to create attributes for the alternate choice that could then be used to run the logit model.

The alternate trip was created such that it passed through the same section of the freeway but on the other set of lanes (ML for GPL trips and GPL for ML trips). The start time of the trip was assumed to be the exact same as the start time of the original trip. The length of the alternate trip could vary a small amount (up to 0.3 miles) depending on the relative location of sensors on both sets of lanes. For alternate trips created on the toll lanes, tolls were assigned depending on the number of toll booths present in the section of the freeway on which the alternate trip was generated.

The travel time for the alternate trip was determined by taking the average of travel times between the given sensor pair during the 15-minute interval in which the actual trip was made. When no trips were observed between a sensor pair in a given interval, then average travel times were used. These average travel times were calculated using actual trips that occurred on these lanes during the same time frame (off-peak, shoulder and peak) on days with travel time data. Table 1 summarizes average speeds used to determine travel times. Standard deviations were calculated the same way.

Period	Average Speed on the Toll Lanes (in mph)	Average Speed on the GPLs (in mph)
Peak Period		
(7–9 a.m. Eastbound and	53.2	42.8
4–6 p.m. Westbound)		
Shoulder		
(6–7 a.m. and 9–10 a.m.		
Eastbound and	61.3	55.6
3–4 a.m. and 6–7 p.m.		
Westbound)		
Off-Peak Period	69 1	65.2
(All Other Times)	68.1	65.3

Note: The speed comparisons are for the entire trip identified, which may include short parts of the trip that are outside the 12 miles of the toll lane.

Lane Changes

Trips that switched between the GPL and ML, or vice versa, during the ML segment of Katy Freeway could not be used. This was because it was impossible to determine the exact location of the lane switch because vehicles were only detected at the sensors, which had fixed locations. This meant travel time savings were impossible to correctly estimate. However, this does not include the longer ML trips that were detected on GPL sensors outside of the 12-mile ML section. For example, ML trips that were detected at GPL sensors 411, 415, 6, 271, etc. (refer to Figure 6) were not deleted. Due to the deletions, the total number of trips in the dataset decreased by 1,259,367.

Trips on the HOV Lane Part of the MLs

The objective of the research was to compare how travelers choose between tolled and toll-free lanes. All trips made on the HOV lanes during the HOV-free times do not pay any tolls but enjoy the same benefits as tolled trips on the toll lanes. Analyzing this third option was beyond the scope of this project and so all trips on the HOV lanes during HOV-free hours were removed. This reduced the total trips for April from 3,530,623 trips to 3,132,295 trips.

Additional Attributes

In addition to the travel time, time of day, day of week, toll, and travel time variability, additional attributes were included to better explain the trip parameters. A variable for heavy rain on the freeway was included (1 if rain was greater than 0.4 inches in that hour and 0 otherwise).

Lane blockages can have an adverse impact on travel time and reliability. Traffic moving from the blocked lanes to the other lanes has the potential to disturb travel time on all the lanes. Therefore, variables were created to account for any lane blockages observed during the trip. The type (ML, GPL, or frontage) and number of lanes blocked were included in the dataset.

Trips were also classified according to the time at which the trip was made. Trips were classified as peak-hour trips, peak-shoulder trips, and off-peak trips. The peak hours were 7 to 9 a.m. eastbound and 4 to 6 p.m. westbound on weekdays. The peak-shoulder hours were 6 to 7 a.m. and 9 to 10 a.m. eastbound and 3 to 4 p.m. and 6 to 7 p.m. westbound on weekdays. All the other times were classified as off-peak.

Final Dataset

The final dataset had two records per trip identified. The two records represented the two potential choices for the trip: one that was made and one on the lanes not chosen. The trip parameters included in the final dataset were the random ID, lane choice, trip time, trip time

standard deviation, total toll paid, trip length, lane blockages, heavy rain, and peak, off-peak, or shoulder period. These attributes were the independent variables used in the logit models.

CHAPTER 5: RESULTS AND INFERENCES

After identifying the trips and the trip attributes, researchers analyzed the data to understand travel behavior on the MLs. First, statistical measures relating to trip attributes were developed to gain preliminary insights into the observed travel trends. Then, logit models were estimated using the available data to further analyze the travel behavior. This chapter discusses the results obtained.

Trips were categorized into peak-period trips, shoulder trips, and off-peak-period trips (see Table 2).

Time Period	Paid Trips*		GPL Trips		Total
Time Feriod	Count	Percentage	Count	Percentage	Trips**
Peak Period					
(7–9 a.m. Eastbound and	92,542	2.95	311,932	9.95	404,474
4–6 p.m. Westbound)					
Shoulder					
(6–7 a.m. and 9–10 a.m.					
Eastbound and	42,665	1.36	304,916	9.73	347,581
3–4 p.m. and 6–7 p.m.					
Westbound)					
Off-Peak Period	00 724	2.90	2 280 506	73.09	2 280 240
(All Other Times)	90,734	2.90	2,289,506	73.09	2,380,240
Total Trips	225,941	7.21	2,906,354	92.79	3,132,295

Table 3: Classification of Trips by Time of Day.

* Paid trips on the MLs made by SOVs and HOVs during non-HOV-free hours

** Total trips excludes trips made by vehicles without transponder IDs, trips on the HOV lanes during HOV-free hours, and trips detected on both MLs and GPLs in the ML portion of the freeway.

The percentage of toll-paying trips made on the MLs decreases from the peak periods to the shoulders to the off-peak periods. This can be attributed to the decreasing travel time savings and decreasing difference in travel time reliability, as shown in Table 3. The numbers for travel time savings and travel time reliability improvement in Table 3 are for the entire trip identified regardless of the length of the trip.

Period	Average Travel Time Savings on the Toll Lanes (in Minutes)	Average Travel Time Reliability Improvement on the Toll Lanes (in Minutes)
Peak Period (7–9 a.m. Eastbound and 4–6 p.m. Westbound)	2.70	0.18
Shoulder (6–7 a.m. and 9–10 a.m. Eastbound and 3–4 a.m. and 6–7 p.m. Westbound)	1.53	0.08
Off-Peak Period (All Other Times)	0.67	0.12

 Table 4: Average Travel Time Savings and Travel Time Reliability Savings by Period.

Average travel time savings for toll-paying trips on the MLs decreases from 2.70 minutes during the peak periods to 0.67 minutes during the off-peak periods. Similarly, the difference in travel time reliability (standard deviation) between MLs and GPLs falls from 0.18 minutes during the peak periods to 0.12 minutes during the off-peak periods though a lowest reliability improvement of 0.08 minutes is observed during the shoulder hours. Considering only the toll-paying trips on the MLs (HOV trips were not included), it would be logical that travelers would be less willing to pay and use the MLs during the off-peak and shoulder periods as compared to peak periods. The speed comparisons are shown in Table 4.

Average speeds increase from the peak periods to shoulders to off-peak periods for both MLs and GPLs. On the other hand, the difference in speeds between MLs and GPLs decreases significantly from the peak to shoulder to off-peak periods.

Based on the travel behavior observed on the freeway, route-choice models were developed, as shown in Equation 6. The multinomal discrete-choice modeling procedure in Statistical Analysis System (SAS) was used to generate the models. These are standard multinomial logit models that attempt to identify what role several factors play in the traveler's lane choice (GPL or ML). Personal information (e.g., gender, age, or income) was not available, and only information on travel conditions, as noted in the previous sections, was used in the models.

$$U_{GPL} = \beta_{TT} TravelTime_{GPL} + \beta_{TTR} TravelTimeReliability_{GPL}$$
$$U_{ML} = \beta_{ML} + \beta_{TolIML} Toll_{ML} + \beta_{TT} TravelTime_{ML} + \beta_{TTR} TravelTimeReliability_{ML}$$
(6)

Where: GPL = general-purpose lane.

ML = managed lane.

Toll = toll paid in the ML. TT = travel time. TTR = travel time reliability.

Models were developed for the whole month, peak periods only, shoulders only, and off-peak periods only. Table 5 shows the results of several models that were generated to potentially explain the travel behavior observed on the freeway.

Intuitively, an increase in toll and travel time should lead to a decrease in utility. In models with only time and toll, negative coefficients were observed for both time and toll. Based on the value of the coefficients, the marginal rate of substitution of time with toll increased from off-peak periods (\$2.60/hour) to shoulder periods (\$8.63/hour) to peak periods (\$10.71/hour). For the entire month, this marginal rate of substitution was \$6.31/hour. This indicates that the relative importance of time with respect to cost (toll) is higher for travelers during the peak periods as compared to the off-peak periods. The addition of an alternate specific coefficient (ASC) to the same time and toll model changes the coefficients drastically. Large negative values of the ML ASC are observed in all models, and the coefficient of toll has a positive value.

VariableAll MonthPeak PeriodShoulderOff-Peak $Model: U_{IOLL} = B_I \times time + B_2 \times toll, U_{GPL} = B_I \times time + B_2 \times toll, (0.001)-0.19-0.29Time-0.26-0.10-0.19-0.29Toll-2.47-0.56-1.32-6.69(0.003)(0.003)(0.005)(0.009)Model: U_{TOLL} = ASC_ML + B_I \times time + B_2 \times toll, U_{GPL} = B_I \times time + B_2 \times toll-4.13ASC_ML-3.75-2.87-3.13-4.13ASC_ML(0.004)(0.010)(0.0010)(0.002)Time-0.16-0.13-0.12-0.25(0.001)(0.001)(0.002)(0.002)Toll0.900.640.661.07(0.003)(0.004)(0.007)(0.012)Model: U_{TOLL} = B_I \times stid + B_2 \times toll, U_{GPL} = B_I \times stid + B_2 \times toll-5.75(Unreliability)(0.005)(0.009)(0.014)(0.011)Model: U_{TOLL} = ASC_ML + B_1 \times stol + B_2 \times toll, U_{GPL} = B_I \times stid + B_2 \times toll-4.02Std Dev.2.310.700.791.51(Unreliability)(0.005)(0.009)(0.014)(0.011)Model: U_{TOLL} = ASC_ML + B_1 \times stol + B_2 \times toll, U_{GPL} = B_1 \times stal + B_2 \times toll-4.02Std. Dev.0.540.340.280.78(Unreliability)(0.006)(0.009)(0.010)(0.001)Model: U_{TOLL} = B_1 \times time + B_2 \times stol + B_3 \times toll, U_{GPL} = B_1 \times time + B_2 \times stol + B_3 \times toll, U_{GPL} = B_1 \times time + B_2 \times stol + B_3 \times toll, U_{GPL} = B_1 \times time + B_2 \times stol + $	X 7. • 11.	Coefficient (Standard Error)			
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Variable	All Month			Off-Peak
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Model: $U_{TOLL} = B_1 \times time + B_2 \times toll, U_{GPL} = B_1 \times time + B_2 \times toll^{\dagger}$				
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$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	1011	(0.003)	(0.003)	(0.005)	(0.009)
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 Table 5: Logit Models Based on Empirical Data.

† The toll for GPL trips was 0.

Similar to time and toll, an increase in the measure of (un)reliability (standard deviation) was also expected to lead to a decrease in the utility. But positive coefficients for standard deviation were observed for all models that included standard deviation of time along with the toll. The addition of an ASC to the standard deviation and toll model also led to high ASC values. This again may be because of the inability of the variables used to correctly model the observed behavior. The models with time, toll, and standard deviation gave similar results with negative coefficients for time and toll when developed without the ASC, and gave high ASC values when developed with the ASC.

As has been noted in transportation literature, toll variables generally have negative coefficients in choice models. As the toll goes up, the utility derived goes down. In the models with the ASC, the tolls do not have positive coefficients in all cases. The toll rate schedule is the same throughout the month except the peak hours and shoulders (four hours) during the weekdays. During the peak hours and shoulders, the toll rates are higher but constant. Therefore, lack of variability in the toll schedule may have led to the model not being able to correctly gauge the impact of toll on lane choice. Also, during the off-peak hours when the tolls are lower, the ridership on the MLs goes down drastically. This means most of the data from travelers making trips on the MLs are during the peak hours. Therefore, limited data on the MLs during the offpeak periods could have hampered the results.

The behavior of travelers on the MLs and how they perceive travel time reliability are also not clear. Even though the standard deviation of travel time is a good measure of the spread of travel time, results show that it may not be how travelers perceive travel time reliability. For a traveler, one bad experience (high delay) on the MLs after having paid a toll may be enough to cause him or her to not use the MLs again for a long time. Also, at the time of making the choice, the decision maker does not have complete information about the travel time and the travel time reliability. Therefore, a large part of the decision-making process is governed by historical data (travel times experienced in the past), which is not accounted for in the model.

It is also possible that Katy Freeway travelers do not make lane choices based on the variables used in this model such as travel time savings or travel time reliability. This may seem like irrational behavior on the part of the travelers, but other factors, such as familiarity in daily travel (lack of willingness to change lanes regularly) and a desire to avoid weaving in and out of MLs, may be more important to these travelers.

Due to the limited entry and exit points in and out of the MLs, travelers may have preferred to stay away from the MLs on short trips and avoid the hassles of weaving in and out of the MLs. Therefore, lane choice could have varied based on the length of the trip. In order to study whether the length of the trip had any impact on how travelers make choices and perceive travel time reliability, the dataset was divided into three categories based on the length of the trips (short, medium, and long). Trips less than 5 miles were categorized as short trips, trips between 5 and 13 miles as medium trips, and trips greater than 13 miles as long trips. Separate models were

developed based on the three datasets, but no significant difference was found based on trip length. Tables 6 and 7 summarize the results of the models generated.

Trin Tune Paid Trips		GPL Trips		Tatal Tring	
Trip Type	Count	Percentage	Count	Percentage	Total Trips
Short (<5 Miles)	63,139	2.02	1,227,636	39.19	1,290,775
Medium (5 to 13 Miles)	120,065	3.83	1,296,555	41.39	1,416,620
Long (>13 Miles)	42,737	1.36	382,163	12.20	424,900
Total Trips	225,941	7.21	2,906,354	92.79	3,132,295

Table 6: Lane Choice Based on Trip Length.

As shown in Table 7, developing models based on the length of the trip had no significant impact on the models. Based on these results, it is clear that travel time, toll, and travel time reliability are not sufficient to explain lane-choice behavior on Katy Freeway. Models were also generated by including additional attributes such as lane blockages and rain, but the results remained largely unchanged.

Because the results obtained were counter-intuitive, it was important to ensure the veracity of the results and the accuracy of the algorithm being used to identify trips and trip attributes. Individual trips were randomly picked and traced back to the original randomized dataset to ensure that the trips were being pieced together correctly. Individual trip attributes such as trip time, trip length, and trip time standard deviation were examined for any anomalies or unexpected trends. The toll values applied on the trips were also cross-checked manually with the prevalent toll schedule at the time the trip was made to ensure the same results were being obtained for all weeks of April were modeled separately to ensure the same results were being obtained for all weeks. A model without any observations in which the trip time standard deviation was approximated using the regression model was also developed. No significant improvement in the model manually. The results were verified with an SAS-generated model to ensure the correct model was being developed.

X 7. • 11.	Coefficient (Standard Error)			
Variable	Short	Medium	Long	
Model: $U_{TOLL} =$	$B_1 \times time + B_2 \times toll, U$	$_{GPL} = B_1 \times time + B_2 \times to$	U U	
Time	0.09	-0.21	-0.33	
	(0.003)	(0.001)	(0.002)	
T-11	-4.09	-1.96	-1.88	
Toll	(0.008)	(0.004)	(0.0054)	
Model: U_{TOLL} =	$ASC_ML + B_1 \times time +$	$B_2 \times toll, U_{GPL} = B_1 \times t$	ime + $B_2 \times toll$	
	-3.60	-3.77	-3.86	
ASC_ML	(0.006)	(0.006)	(0.011)	
Time	-0.10	-0.15	-0.18	
Time	(0.002)	(0.001)	(0.002)	
Toll	0.70	0.98	0.99	
1011	(0.005)	(0.004)	(0.007)	
Model: U_{TOLL} =	$B_1 \times std + B_2 \times toll, U_G$	$PL = \overline{B_1 \times std} + B_2 \times toll$		
Std. Dev.	2.29	2.61	2.20	
(Unreliability)	(0.016)	(0.008)	(0.012)	
Toll	-3.86	-1.08	-0.78	
1011	(0.007)	(0.003)	(0.004)	
Model: U_{TOLL} =	$ASC_ML + B_1 \times std +$	$B_2 \times toll, U_{GPL} = B_1 \times sta$	$d + B_2 \times toll$	
ASC_ML	-3.50	-3.64	-3.77	
ASC_ML	(0.006)	(0.006)	(0.010)	
Std. Dev.	0.86	0.58	0.48	
(Unreliability)	(0.016)	(0.008)	(0.013)	
Toll	0.78	1.25	1.34	
1011	(0.005)	(0.003)	(0.006)	
Model: U_{TOLL} =	$B_1 \times time + B_2 \times std + B_2$	$B_3 \times toll, U_{GPL} = B_1 \times time$	$e + B_2 \times std + B_3 \times toll$	
Time	-0.01	-0.25	-0.38	
	(0.003)	(0.001)	(0.002)	
Std. Dev.	2.30	2.65	2.46	
(Unreliability)	(0.016)	(0.008)	(0.013)	
Toll	-3.88	-1.53	-1.51	
	(0.008)	(0.004)	(0.006)	
Model: U_{TOLL} =	$ASC_ML + B_1 \times time +$	$+B_2 \times std + B_3 \times toll, U_T$	$B_{OLL} = B_1 \times time +$	
$B_2 \times std + B_3 \times tot$	11	I		
ASC_ML	-(0.006)	-3.65	-3.68	
		(0.006)	(0.011)	
Time	-0.15	-0.16	-0.20	
	(0.003)	(0.001)	(0.002)	
Std. Dev.	1.06	0.73	0.81	
(Unreliability)	(0.016)	(0.009)	(0.014)	
Toll	0.69	0.98	0.96	
1011	(0.006)	(0.004)	(0.007)	

Table 7: Logit Models Based on Trip Lengths.
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As discussed previously, other personal attributes such as age, gender, income, and attitude toward risk were not available and hence could not be accounted for in the study. The presence of these variables and their interactions with existing variables could have helped better explain the behavior of travelers and their choices.

CHAPTER 6: CONCLUSIONS AND FUTURE WORK

The objective of this project was to study and analyze the travel behavior of Katy Freeway travelers using empirical data obtained from their trips on Katy Freeway. Lane-choice logit models were developed to study the behavior and attributes that influenced lane-choice decisions.

Based on the data, it was found that most paid trips on the paid MLs occurred during the peak hours. The number of ML trips decreased during the shoulder periods and further decreased during the off-peak periods. This was in agreement with the decreased travel time savings and decreased travel time reliability savings that existed off-peak.

Models were developed to explain the observed behavior on the freeway. These included various combinations of travelers' travel time, travel time reliability, and toll paid. None of the models were able to conclusively explain the observed behavior on the freeway. Most models had positive coefficients for toll and reliability (travel time standard deviation), suggesting an increase in toll or an increase in travel time variability increased utility. This is contrary to how rational travelers perceive these attributes. Only in the time and toll model (without an ASC) were negative coefficients observed for both time and toll. These models yielded reasonable values of time of \$2.60/hour, \$8.63/hour, and \$10.71/hour for off-peak-period, shoulder, and peak-period travelers, respectively. Also, it was observed that the addition of an ASC to models led to relatively high ASC values (in magnitude) compared to other attribute coefficients. This implies that there was a weak relationship between lane choice and other model attributes.

Different models were also developed based on the length of the trip to evaluate if behavior changed with a change in trip length. No significant differences were found in the different models; only minor variations in the magnitude of attribute coefficients were found.

The inability of the models to provide more intuitive results could have several potential causes. These can be broadly categorized as data specific and model specific. The lack of sufficient variation in the toll schedule and the low number of trips observed on the MLs during shoulder periods and off-peak periods are issues related to the empirical data used. These could have potentially impacted the results of the models. The models were unable to conclusively explain the behavior observed on the freeway, and therefore the additional attributes may be needed to better explain the observed behavior. Also, the standard deviation may not be the best measure of travelers' perception of travel time reliability. Other measures may better represent how travelers perceive reliability.

A lack of clarity on how travelers perceive travel time reliability hampers travel time reliability studies. Further research is needed to understand the measure of travel time reliability that best represents travelers' perception of reliability. The standard deviation of travel time was used as the attribute representing reliability. Other measures of reliability that could be considered

include interquartile ranges of travel time distributions (e.g., the difference between 90th and 50th percentile), number of bad trips in the last 20 trips (e.g., a bad trip could be defined as a trip with a travel time greater than twice the average travel time), and others.

Also, in order to study some of these reliability measures and to better understand travel behavior, it is important to track trips over a longer period of time. Due to computational limitations, only a month of data could be used for this project. But tracking and analyzing trips over a longer period of time would potentially give better insights into how travelers make decisions on the freeway.

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